

# Power Grid Frequency Increments as Indicators of Complex and Critical Dynamics in Networked Systems

G. Cigdem Yalcin<sup>1</sup>, Christian Beck<sup>2</sup>, Benjamin Schäfer<sup>3</sup>, Xinyi Wen<sup>3</sup>, Mehrnaz Anvari<sup>4</sup>, Jacques Maritz<sup>5</sup>, Leonardo Rydin Gorjão<sup>6,7</sup>

<sup>1</sup> Department of Physics, Faculty of Science, Istanbul University, 34134, Vezneciler, Istanbul, Turkiye

<sup>2</sup> School of Mathematical Sciences, Queen Mary University of London, London, UK

<sup>3</sup> Institute for Automation and Applied Informatics, Karlsruhe Institute of Technology, Eggenstein-Leopoldshafen, Germany

<sup>4</sup> Fraunhofer Institute for Algorithms and Scientific Computing SCAI, Germany

<sup>5</sup> Department of Engineering Sciences, University of the Free State, Bloemfontein 9301, South Africa

<sup>6</sup> Department of Environmental Sciences, Faculty of Science, Open University, Heerlen, The Netherlands

<sup>7</sup> Faculty of Science and Technology, Norwegian University of Life Sciences, 1432 Ås, Norway

## Abstract

Power grids are a good example of a human-made complex system that is vital for the functioning of many supply systems crucial to our lives. On the one hand, they generate complex frequency fluctuation signals at the micro scale, and on the other hand they represent complex network topologies at the macro scale [1,2]. A limited number of studies have been conducted to create open databases of power grid frequencies from various locations in continental Europe and to analyse them using real experimental data [3]. Nevertheless, in a very recent study, real power grid frequency data recorded from Asia, Australia, and Europe were analyzed for their non-standard characteristics, and for the first time, an open data source for these regions was created [4].

In this study, we show that the PDFs of the increments of power grid frequency data recently recorded in regions across Asia, Australia, Africa and Europe, exhibit a non-Gaussian distribution. In addition, we apply q-Gaussian fits to demonstrate that they display fat tails that are characterized by a q-Gaussian equation, a feature that is consistently identified as a typical characteristics of complex behavior. Some of the distributions that we investigate also exhibit slightly asymmetric behaviour.

[1] Benjamin Schäfer, G. Cigdem Yalcin, Dynamical modeling of cascading failures in the Turkish power grid. *Chaos*, 29 (9): 093134, (2019)

[2] Benjamin Schäfer, Leonardo Rydin Gorjão, G.Cigdem Yalcin, Ellen Förstner, Richard Jumar, Heiko Maass, Uwe Kühnapfel, Veit Hagenmeyer, Microscopic fluctuations in power-grid frequency recordings at the subsecond scale, *Complexity*, 2023, 2657039, (2023).

[3] L. Rydin Gorjão, R. Jumar, H. Maass, V. Hagenmeyer, G. C. Yalcin, J. Kruse, M. Timme, C. Beck, D. Witthaut, B. Schäfer, Open database analysis of scaling and spatio-temporal properties of power grid frequencies. *Nat Commun* 11, 6362 (2020).

[4] Xinyi Wen, Mehrnaz Anvari, Leonardo Rydin Gorjao, G.Cigdem Yalcin, Veit Hagenmeyer, Benjamin Schafer, Non-standard power grid frequency statistics in Asia, Australia, and Europe, (arxiv.org/abs/2308.16842), (2024).